Please check the examination details below before entering your candidate information


Mock Paper

## Mathematics

Advanced
Paper 3B - Mechanics

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You must have:
Mathematical Formulae and Statistical Tables, calculator
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Total Marks

Candidates may use any calculator allowed by Pearson regulations.
Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

Use black ink or ball-point pen.
If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
Fill in the boxes at the top of this page with your name, centre number and candidate number.
Answer all questions and ensure that your answers to parts of questions are clearly labelled. Answer the questions.
You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
Inexact answers should be given to three significant figures unless otherwise stated.

## Information

A booklet 'Mathematical Formulae and Statistical Tables' is provided.
There are 9 questions in this question paper. The total mark for this paper is 104.
The marks for each question are shown in brackets

- use this as a guide as to how much time to spend on each question.


## Advice

Read each question carefully before you start to answer it.
Try to answer every question.
Check your answers if you have time at the end.
1.


Figure 1
A uniform wooden beam $A B$, of mass 20 kg and length 4 m , rests in equilibrium in a horizontal position on two supports. One support is at $C$, where $A C=1.6 \mathrm{~m}$, and the other support is at $D$, where $D B=0.4 \mathrm{~m}$. A boy of mass 60 kg stands on the beam at the point $P$, where $A P=3 \mathrm{~m}$, as shown in Figure 1. The beam remains in equilibrium in a horizontal position.

By modelling the boy as a particle and the beam as a uniform rod,
(a) (i) find, in terms of $g$, the magnitude of the force exerted on the beam by the support at $C$,
(ii) find, in terms of $g$, the magnitude of the force exerted on the beam by the support at $D$.

The boy now starts to walk slowly along the beam towards the end $A$.
(b) Find the greatest distance he can walk from $P$ without the beam tilting.
2. A cyclist starts from rest at the point $O$ on a straight horizontal road. The cyclist moves along the road with constant acceleration $2 \mathrm{~m} \mathrm{~s}^{-2}$ for 4 seconds and then continues to move along the road at constant speed. At the instant when the cyclist stops accelerating, a motorcyclist starts from rest at the point $O$ and moves along the road with constant acceleration $4 \mathrm{~m} \mathrm{~s}^{-2}$ in the same direction as the cyclist. The motorcyclist has been moving for $T$ seconds when she overtakes the cyclist.
(a) Sketch, on the same axes, a speed-time graph for the motion of the cyclist and a speed-time graph for the motion of the motorcyclist, to the time when the motorcyclist overtakes the cyclist.
(b) Find, giving your answer to 1 decimal place, the value of $T$.
3. A rough plane is inclined at an angle $\alpha$ to the horizontal, where $\tan \alpha=\frac{3}{4}$. A particle of mass 2 kg is projected with speed $6 \mathrm{~m} \mathrm{~s}^{-1}$ from a point $O$ on the plane, up a line of greatest slope of the plane. The coefficient of friction between the particle and the plane is 0.25
(a) Find the magnitude of the frictional force acting on the particle as it moves up the plane.

The particle comes to instantaneous rest at the point $A$.
(b) Find the distance $O A$.

The particle now moves down the plane from $A$.
(c) Find the speed of $P$ as it passes through $O$.
(Total 13 marks)
4. [In this question $\mathbf{i}$ and $\mathbf{j}$ are perpendicular horizontal unit vectors and position vectors are given relative to a fixed origin $O$.]

A particle $P$ is moving in a straight line with constant velocity. At 9 am, the position vector of $P$ is $(7 \mathbf{i}+5 \mathbf{j}) \mathrm{km}$ and at 9.20 am , the position vector of $P$ is $6 \mathbf{i} \mathrm{~km}$. At time $t$ hours after 9 am , the position vector of $P$ is $\mathbf{r}_{P} \mathrm{~km}$.
(a) Find, in $\mathrm{km} \mathrm{h}^{-1}$, the speed of $P$.
(b) Show that $\mathbf{r}_{P}=(7-3 t) \mathbf{i}+(5-15 t) \mathbf{j}$.
(c) Find the value of $t$ when $\mathbf{r}_{P}$ is parallel to $16 \mathbf{i}+5 \mathbf{j}$.

The position vector of another particle $Q$, at time $t$ hours after 9 am , is $\mathbf{r}_{Q} \mathrm{~km}$, where $\mathbf{r}_{Q}=(5+2 t) \mathbf{i}+(-3+5 t) \mathbf{j}$
(d) Show that $P$ and $Q$ will collide and find the position vector of the point of collision.
5. A car pulls a trailer along a straight horizontal road using a light inextensible towbar. The mass of the car is $M \mathrm{~kg}$, the mass of the trailer is 600 kg and the towbar is horizontal and parallel to the direction of motion. There is a resistance to motion of magnitude 200 N acting on the car and a resistance to motion of magnitude 100 N acting on the trailer.

The driver of the car spots a hazard ahead. Instantly he reduces the force produced by the engine of the car to zero and applies the brakes of the car. The brakes produce a braking force on the car of magnitude 6500 N and the car and the trailer have a constant deceleration of magnitude $4 \mathrm{~m} \mathrm{~s}^{-2}$.

Given that the resistances to motion on the car and trailer are unchanged and that the car comes to rest after travelling 40.5 m from the point where the brakes were applied, find
(a) the thrust in the towbar while the car is braking,
(b) the value of $M$,
(c) the time it takes for the car to stop after the brakes are applied.
6.


## Figure 2

A washing line $A B C D$ is fixed at the points $A$ and $D$. There are two heavy items of clothing hanging on the washing line, one fixed at $B$ and the other fixed at $C$. The washing line is modelled as a light inextensible string, the item at $B$ is modelled as a particle of mass 3 kg and the item at $C$ is modelled as a particle of mass $M \mathrm{~kg}$. The section $A B$ makes an angle $\alpha$ with the horizontal, where $\tan \alpha=\frac{3}{4}$, the section $B C$ is horizontal and the section $C D$ makes an angle $\beta$ with the horizontal, where $\tan \beta=\frac{12}{5}$, as shown in Figure 2. The system is in equilibrium.
(a) Find the tension in $A B$.
(b) Find the tension in BC.
(c) Find the value of $M$.
7.


Figure 3
A uniform rod $A B$, of mass 6 kg and length 1.6 m , rests with its end $A$ on rough horizontal ground. The rod is held in equilibrium at $30^{\circ}$ to the horizontal by a light string attached to the rod at $B$. The string is at $40^{\circ}$ to the horizontal and lies in the same vertical plane as the rod, as shown in Figure 3. The tension in the string is $T$ newtons. The coefficient of friction between the ground and the rod is $\mu$.
(a) Show that, to 3 significant figures, $T=27.1$
(b) Find the set of values of $\mu$ for which equilibrium is possible.
(Total 9 marks)
8. A particle $P$ of mass 0.3 kg moves under the action of a single force $\mathbf{F}$ newtons. At time $t$ seconds ( $t \geq 0$ ), $P$ has velocity $\mathbf{v ~ m ~ s}{ }^{-1}$, where

$$
\mathbf{v}=\left(3 t^{2}-4 t\right) \mathbf{i}+\left(3 t^{2}-8 t+4\right) \mathbf{j}
$$

(a) Find $\mathbf{F}$ when $t=4$

At the instants when $P$ is at the points $A$ and $B$, particle $P$ is moving parallel to the vector $\mathbf{i}$.
(b) Find the distance $A B$.
9. A particle $P$ is projected from a fixed point $A$ with speed $12 \mathrm{~m} \mathrm{~s}^{-1}$ at an angle $\alpha$ above the horizontal and moves freely under gravity. As $P$ passes through the point $B$ on its path, $P$ is moving with speed $8 \mathrm{~m} \mathrm{~s}^{-1}$ at an angle $\beta$ below the horizontal.
(a) By considering energy, find the vertical distance between $A$ and $B$.
(4)

Particle $P$ takes 1.5 seconds to travel from $A$ to $B$.
(b) Find the size of angle $\alpha$.
(3)
(c) Find the size of angle $\beta$.
(d) Find the length of time for which the speed of $P$ is less than $8 \mathrm{~m} \mathrm{~s}^{-1}$.

