## Mark Scheme (Results)

January 2019

Pearson Edexcel International Advanced Level In Mechanics M1 (WME01/01)

| Question | Scheme | Marks |
| :---: | :---: | :---: |
| 2(a) | $\begin{aligned} & \tan \theta=\frac{6}{7} \\ & \theta=40.60^{\circ} \ldots \end{aligned}$ <br> Bearing is $360^{\circ}-40.60^{\circ}=319^{\circ}$ nearest degree | M1 <br> A1 <br> A1 <br> (3) |
| (b) | $\begin{aligned} & \mathbf{r}_{A}=(20 \mathbf{i}-17 \mathbf{j})+4(-6 \mathbf{i}+7 \mathbf{j})=(-4 \mathbf{i}+11 \mathbf{j}) \\ & \mathbf{r}_{B}=(-8 \mathbf{i}+9 \mathbf{j})+4(p \mathbf{i}+2 p \mathbf{j})=(-8+4 p) \mathbf{i}+(9+8 p) \mathbf{j} \\ & \mathbf{r}_{A}-\mathbf{r}_{B}=(4-4 p) \mathbf{i}+(2-8 p) \mathbf{j} \\ &-8+4 p--4=9+8 p-11 \\ & \quad p=-0.5 \\ & \mathbf{v}_{B}=(-0.5 \mathbf{i}-\mathbf{j}) \\ &\left\|\mathbf{v}_{B}\right\|=\sqrt{(-0.5)^{2}+(-1)^{2}} \\ &=\frac{\sqrt{5}}{2}=1.1 \mathrm{~ms}^{-1} \text { or better } \end{aligned}$ | M1 A1  <br> A1  <br> DM1  <br> M1 A1  <br> A1  <br> M1  <br> M1  <br> A1 $(10)$ <br>  13 |
|  | Notes |  |
| 2(a) | M1 for any trig ratio using 6 and 7: $\tan \theta= \pm \frac{6}{7}$ or $\pm \frac{7}{6}: \sin \theta$ or $\cos \theta= \pm \frac{6}{\sqrt{6^{2}+7^{2}}}$ or $\pm \frac{7}{\sqrt{6^{2}+7^{2}}}$ |  |
|  | A1 for a correct angle from their correct equation e.g. $49^{\circ}, 41^{\circ}, 139^{\circ}, 131^{\circ}, \ldots$. |  |
|  | A1 for $319^{\circ}$ cao |  |
| 2(b) | First M1 for attempt at use of $\mathbf{r}_{4}=\mathbf{r}_{0}+4 \mathbf{v}$ for either $A$ or $B$ |  |
|  | First A1 for ( $-4 \mathbf{i}+11 \mathbf{j}$ ) ${ }^{\text {inds }}$ and $\mathbf{j}$ 's must be collected at some stage |  |
|  | Second A1 for $(-8+4 p) \mathbf{i}+(9+8 p) \mathbf{j} \quad \mathbf{i}$ 's and $\mathbf{j}$ 's must be collected at some stage |  |
|  | Second DM1, dependent on first M1, for finding the difference between their two $\mathbf{r}_{4}$ vectors (must be an attempt to subtract both $\mathbf{i}$ and $\mathbf{j}$ components) |  |
|  | Third M1 for equating the $\mathbf{i}$ cpt and $\mathbf{j}$ cpt of their difference (M0 if no difference) to give an equation in $p$ only. oe $\text { e.g. } \frac{(4-4 p)}{(2-8 p)}=\frac{(-) 1}{(-) 1}$ |  |
|  | Third A1 for a correct equation in $p$ only |  |
|  | Fourth A1 for a correct value of $p$ |  |
|  | Fourth M1 for using their $p$ value to obtain a velocity vector for $B$ |  |
|  | Fifth M1 for finding the magnitude of their $\mathbf{v}_{B}$ (N.B. This M mark is available, even if their $\mathbf{v}_{B}$ does not have the correct form) |  |
|  | Fifth A1 for $\frac{\sqrt{5}}{2}$ oe or 1.1 or better |  |


| Question | Scheme | Marks |
| :---: | :---: | :---: |
| 3(a) | $560-m g=1.4 m$ | M1 A1 (2) |
| (b) | $2800-M g-560=1.4 M$ | M1 A1 (2) |
| (c) (i) <br> (ii) | $\begin{aligned} 560 & =11.2 m \\ m & =50 \\ 2240 & =11.2 M \\ M & =200 \end{aligned}$ | $\begin{array}{lll} \hline \text { DM1 } & \\ \text { A1 } & \\ \text { A1 } & \text { (3) } 7 \end{array}$ |
|  | Notes |  |
| (a) | M1 for equation of motion for the person only, with usual rules, condone sign errors, and with at least one value ( 560 or 1.4) substituted. Credit given for this equation only if it appears in (a). |  |
|  | A1 for a correct equation |  |
| (b) | M1 for equation of motion for the lift only, with usual rules, condone sign errors, and with at least one value $(2800,560$ or 1.4 ) substituted. Credit given for this equation only if it appears in (b). |  |
|  | A1 for a correct equation |  |
| (c) | Hence: <br> DM1, dependent on appropriate previous M mark, for solving one of their equations, wherever it appears, for either $m$ or $M$ <br> Otherwise: <br> DM1, dependent on appropriate previous M mark, for solving one of their equations and/or the whole system equation, wherever they appear, for either $m$ or $M$ <br> N.B. There are no marks available for the whole system equation |  |
|  | First A1 for $m=50$ |  |
|  | Second A1 for $M=200$ |  |


| Question | Scheme | Marks |
| :---: | :---: | :---: |
| 4(a) | $\begin{aligned} & M(R), 40 g(x-3)+2.5 g \times 2=30 g \times 0.5 \\ & x=3.25 \mathrm{~m} \text { from } P \end{aligned}$ | M1 A2 A1 <br> (4) |
| (b) | Mass of the box is concentrated at the point $Q$ oe | B1 (1) |
| (c) | $\begin{aligned} M(R), 3 M g+30 g \times 0.5 & =2.5 g \times 2+40 g \times 2 \\ M & =\frac{70}{3}, 23 \text { or better } \end{aligned}$ | M1 A2 <br> A1 <br> (4) $9$ |
|  | Notes |  |
| 4(a) | M1 for moments about $R$ to give an equation in $x$ (or another unknown distance) only (i.e. M0 if reaction at $P$ is non-zero) Correct no. of terms, dimensionally correct |  |
|  | A2 for a correct equation in $x$ only (allow consistent omission of $g$ ) -1 each error |  |
|  | Alternative: Instead of $M(R)$, they may write down 2 equations and eliminate the normal reaction at $R, N_{R}$, to obtain an equation in a distance only: <br> Possible equations: $\begin{aligned} & (\uparrow) N_{R}=40 g+30 g+2.5 g \\ & M(P), 40 g x+30 g \times 2.5+2.5 g \times 5=3 N_{R} \end{aligned}$ $\begin{aligned} & M(Q), 40 g(5-x)+30 g \times 2.5=2 N_{R} \\ & M(G), 40 g(2.5-x)+0.5 N_{R}=2.5 g \times 2.5 \end{aligned}$ <br> Equations must have correct no. of terms and be dimensionally correct but M0 if reaction at $P$ is non-zero |  |
|  | Third A1 for $\frac{13}{4} \mathrm{~m}$ oe Allow 3.3 m |  |
| (b) | B1 for mass or weight of box acts at $Q$ but B0 if extra wrong answers |  |
| (c) | M1 for moments about $R$ to give an equation in $M$ only (i.e. M0 if reaction at $P$ is non-zero) Correct no. of terms, dimensionally correct |  |
|  | A2 for a correct equation in M only (allow consistent omission of $g$ ) -1 each error |  |
|  | Alternative: Instead of $M(R)$, they may write down 2 equations and eliminate the normal reaction at $R, S_{R}$, to obtain an equation in $M$ only : <br> Possible equations: $\begin{aligned} & (\uparrow) S_{R}=40 g+30 g+2.5 g+M g \\ & M(P), 42.5 g \times 5+30 g \times 2.5=3 S_{R} \end{aligned}$ $\begin{aligned} & M(Q), M g \times 5+30 g \times 2.5=2 S_{R} \\ & M(G), M g \times 2.5+0.5 S_{R}=42.5 g \times 2.5 \end{aligned}$ <br> Equations must have correct no. of terms and be dimensionally correct but M0 if reaction at $P$ is non-zero |  |
|  | Third A1 for $\frac{70}{3}$ oe or 23 or better Accept 24 |  |


| Question <br> Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. | $\begin{aligned} & P M=3.5-2 \tan 45^{\circ}=1.5 \quad \text { OR } P B=\sqrt{3.5^{2}+\left(\frac{2}{\sin 45}\right)^{2}-2 \times 3.5 \times\left(\frac{2}{\sin 45}\right) \cos 45^{\circ}}=2.5 \\ & \quad \tan \alpha=\frac{1.5}{2} ; \cos \alpha=\frac{4}{5} ; \sin \alpha=\frac{3}{5} \\ & \text { OR } \quad \alpha=37^{\circ} \text { or } \quad\left(90^{\circ}-\alpha\right)=53^{\circ} \quad \text { (at least 2SF) } \end{aligned}$ $\begin{aligned} & T_{P} \cos \alpha+T_{Q} \cos 45^{\circ}=6 \mathrm{~g} \\ & T_{P} \sin \alpha=T_{Q} \cos 45^{\circ} \\ & T_{P}=\frac{30 g}{7}=42 \mathrm{~N} ; \quad T_{Q}=36 \text { or } 35.6 \mathrm{~N} \end{aligned}$ | M1 <br> A1 <br> M1 A2 -1 ee <br> M1 A1 <br> DM1 A1; A1 |
|  | Notes |  |
|  | First M1 for finding the length of $P M$ or $P B$ |  |
|  | First A1 for a correct trig ratio for $\alpha$ or $\left(90^{\circ}-\alpha\right)$ or a correct value for $\alpha$ or $\left(90^{\circ}-\alpha\right)$ Do not penalise accuracy here if their final answers for the tensions are correct. |  |
|  | N.B. If they assume the tensions are the same, no further marks available If they think $\alpha=30$ or 60 or....., they could get all 5 resolving marks as a value of $\alpha$ is not required but if $\alpha=\mathbf{4 5}$, only M marks available. However, if $\alpha$ and 45 are interchanged in the resolving equations - no marks available for resolving |  |
|  | Second M1 for resolving vertically with usual rules |  |
|  | Second/Third A1's for a correct equation, ( $\alpha$ does not need to be substituted) -1 each error |  |
|  | Third M1 for resolving horizontally with usual rules |  |
|  | Fourth A1 for a correct equation ( $\alpha$ does not need to be substituted but if it is , follow through on their value) |  |
|  | Fourth DM1, dependent on all THREE previous M marks, for solving for either tension |  |
|  | Fifth A1 for $T_{P}$ Allow $42.0 \quad$ Units not needed |  |
|  | Sixth A1 for $T_{Q}$ Units not needed |  |
|  | Alternative, using Triangle of Forces/Lami's Theorem, for middle 5 marks. |  |
|  | $\frac{T_{P}}{\sin 45^{\circ}}=\frac{6 g}{\sin \left(45^{\circ}+\alpha\right)} \quad \text { OR } \quad \frac{T_{Q}}{\sin \left(180^{\circ}-\alpha\right)}=\frac{6 g}{\sin \left(45^{\circ}+\alpha\right)}$ | M1 A2 -1 ee |
|  | $\frac{T_{Q}}{\sin \left(180^{\circ}-\alpha\right)}=\frac{6 g}{\sin \left(45^{\circ}+\alpha\right)} \quad$ OR $\quad \frac{T_{P}}{\sin 45^{\circ}}=\frac{6 g}{\sin \left(45^{\circ}+\alpha\right)} \quad$ OR $\frac{T_{P}}{\sin 45^{\circ}}=\frac{T_{Q}}{\sin \left(180^{\circ}-\alpha\right)}$ | M1 A1 |
|  | N.B. Treat omission of $g$ as one error |  |
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| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 6(a) |  | B1 Shape <br> B1 Figs. and $V$ <br> (2) |
| (b) | $\begin{gathered} 4500=\frac{(270+180)}{2} V \quad \text { OR } \quad 4500=\frac{1}{2} 60 V+180 V+\frac{1}{2} 30 V \\ V=20 \end{gathered}$ | M1 A1 <br> A1 <br> (3) |
| (c) | $\begin{gathered} \frac{(T+T-60)}{2} \times 20=2250 \quad \text { OR } \quad \frac{1}{2} 60.20+(T-60) \cdot 20=2250 \\ T=142.5 \mathrm{~s} \end{gathered}$ | M1 A2 ft <br> A1 <br> (4) |
| (d) | $\begin{aligned} T_{1} & =\frac{1}{4} \times 60 \\ & =15 \end{aligned}$ $\begin{aligned} T_{2}=270-\left(\frac{1}{4} \times 30\right) & \text { OR } \quad 240+\left(\frac{3}{4} \times 30\right) \\ & =262.5 \end{aligned}$ | M1 A1 <br> M1 A1 <br> A1 <br> (5) |
|  | Notes |  |
| 6(a) | First B1 for a trapezium (not to scale) starting and finishing on the $t$-axis but B0 if solid vertical lines included |  |
|  | Second B1 for 3 figs. (60, 270 and use of 30 with a delineator or 240) and $V$. 270 can be implied by 3 correct delineators |  |
| 6(b) | M1 for a complete method to produce an equation, in $V$ only, with the correct structure i.e. one trapezium <br> or two triangles + rectangle <br> or triangle + trapezium <br> or trapezium + triangle <br> or rectangle - two triangles $=4500$ (allow 4.5 for the M mark) <br> (M0 if a single suvat equation is used) |  |
|  | First A1 for a correct unsimplified equation |  |
|  | Second A1 for $V=20$ |  |
| 6(c) | M 1 for a complete method to produce an equation, in ONE variable e.g. $t$ where $t=(T-60)$, with the correct structure <br> i.e. one trapezium <br> or triangle + rectangle <br> or rectangle - triangle $\quad=2250 \quad$ (allow 2.25 for the M mark) <br> (M0 if a single suvat equation is used) |  |
|  | First and second A1's for a correct unsimplified equation ft on their $20-1$ each error |  |
|  | Third A1 for 142.5 (s) cao Accept 143. |  |
| 6(d) | First M1 for a complete method to give an equation in $T_{1}$ only |  |


|  | First A1 for 15 (independent of $V$ so allow even if their $V$ is wrong) |  |
| :--- | :--- | :--- |
|  | Second M1 for a complete method to give an equation in $T_{2}$ only |  |
|  | Second A1 for a correct equation |  |
|  | Third A1 for 262.5 (independent of $V$ so allow even if their $V$ is wrong) Accept 263 |  |
|  | N.B. Accept $T_{1}=262.5$ and $T_{2}=15$ |  |
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|  | Special Case: Allow max M1A1DM0A0 if $\boldsymbol{m}$ is lost from their $\boldsymbol{T}$ but expression for $\boldsymbol{R}$ <br> is otherwise correct. |  |
| :--- | :--- | :--- |
|  | First A1 for a correct expression for $R$ in terms of $T$ and $\alpha$ |  |
|  | Second DM1 for substituting in their expression for $T$ and a correct value for $\alpha$ but must <br> be in terms of $m$ |  |
|  | Second A1 for a correct answer (any equivalent surd form) |  |
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Mark Scheme (Results)

January 2019

Pearson Edexcel International Advanced Level In Mechanics M2 (WME02/01)

| Q | Scheme | Marks | Notes |
| :---: | :---: | :---: | :---: |
| 5 | Differentiate to find $a$ : | M1 | Powers going down |
|  | $a=\frac{\mathrm{d} v}{\mathrm{~d} t}=3 t^{\frac{1}{2}}-6$ | A1 |  |
|  | Solve for $a=0$ : | M1 |  |
|  | $t^{\frac{1}{2}}=2 \Rightarrow t=4$ | A1 |  |
|  | Integrate to find $s$ : $s=\int v \mathrm{~d} t$ | M1 | Powers going up |
|  | $=\frac{4}{5} t^{\frac{5}{2}}-3 t^{2}+2 t(+C)$ | A1 |  |
|  | Use limits 0 and their 4: $s=\frac{4}{5} \times 32-48+8(=-14.4)$ | DM1 | Limits used correctly Use of 0 can be implied Dependent on the preceding M1 |
|  | Distance $=14.4$ (m) (14 (m) $)$ | A1 | Or equivalent. Positive answer required |
|  |  | (8) |  |
|  |  | [8] |  |
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| Q | Scheme | Marks | Notes |
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| 6a |  |  |  |
|  | Moments about $A$ : | M1 | Dimensionally correct. Condone $\sin / \mathrm{cos}$ confusion |
|  | $2.5 N=2 \cos \theta \times 20$ | A1 | Correct unsimplified equation |
|  | $N=\frac{2 \times \frac{4}{5} \times 20}{2.5}=12.8(\mathrm{~N})$ | A1 | $\text { Accept } \frac{64}{5}$ |
|  |  | (3) |  |
| 6b | Resolve $\downarrow: R+N \cos \theta+P \sin \theta=20$ | M1 | 1st equation. Dimensionally correct. Condone $\sin /$ cos confusion and sign errors |
|  | $(R=9.76-0.6 P)$ | A1ft | Correct unsimplified equation in $N$ or their $N$ |
|  | Resolve $\leftrightarrow: F+P \cos \theta=N \sin \theta$ | M1 | 2nd equation. Dimensionally correct. Condone $\sin / \cos$ confusion and sign errors |
|  | $(F=7.68-0.8 P)$ | A1ft | Correct unsimplified equation in $N$ or their $N$ |
|  | Use $F=\frac{1}{4} R$ : | B1 |  |
|  | Equation in $P$ only: $7.68-0.8 P=\frac{1}{4}(9.76-0.6 P)$ ( $P=8.06 \ldots$...) | DM1 | (or eliminate $P$ ) <br> Dependent on the preceding 2 M marks |
|  | Solve for $\mu$ : $P=\mu N$ | DM1 | Dependent on the preceding M mark |
|  | $\mu=0.630, \quad(0.63)$ | A1 | 0.63 or better |
|  |  | (8) |  |
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|  |  |  | See over for alternatives |
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| Q | Scheme | Marks | Notes |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \mathbf{6 b} \\ & \text { alt } \end{aligned}$ | Moments about $C$ : $20 \times 0.5 \cos \theta+F \times 2.5 \sin \theta=R \times 2.5 \cos \theta$ | M1 | $1^{\text {st }}$ equation. Dimensionally correct. Condone $\sin /$ cos confusion and sign errors |
|  | $(40+7.5 F=10 R)$ | A1 | Correct unsimplified equation |
|  | Resolve parallel rod: | M1 | $2^{\text {nd }}$ equation. Dimensionally correct. Condone $\sin /$ cos confusion and sign errors |
|  | $P+F \cos \theta+R \sin \theta=20 \sin \theta(=12)$ | A1 | Correct unsimplified equation |
|  | Use $F=\frac{1}{4} R:(8.125 R=40, \quad R=4.92 \ldots)$ | B1 |  |
|  | Solve for $P$ : $P=12-\frac{R}{4} \times \frac{4}{5}-R \times \frac{3}{5}=12-\frac{4}{5} R=8.06 \ldots$ | DM1 | Dependent on the preceding 2 M marks |
|  | Solve for $\mu: \quad P=\mu N$, | DM1 | Dependent on the preceding M mark |
|  | $\mu=0.630 \quad$ (0.63) | A1 |  |
|  |  | (8) |  |
|  |  |  |  |
| 6alt | If the use of moments about $C$ is part of the solution to (a) |  |  |
|  | Moments about $C$ and use : $20 \times 0.5 \cos \theta+F \times 2.5 \sin \theta=R \times 2.5 \cos \theta$ | M1 | From (b) Dimensionally correct. Condone $\sin / \cos$ confusion and sign errors |
|  | Use of $F=\frac{1}{4} R$ | B1 | From (b) |
|  | $R=\frac{64}{13}, \quad(R=4.92 \ldots)$ | A1 | From (b) |
|  | Resolve perpendicular to the rod: | M1 | *From (a) |
|  | $N+R \cos \theta=\mu R \sin \theta+W \cos \theta$ | A1 | From (a) Correct unsimplified equation |
|  | $N=12.8$ (N) | A1 | From (a) |
|  | Resolve parallel rod: | M1 | *Dimensionally correct. Condone $\sin / \mathrm{cos}$ confusion and sign errors |
|  | $P+F \cos \theta+R \sin \theta=20 \sin \theta(=12)$ | A1 | Correct unsimplified equation |
|  | Solve for $P$ : $P=12-\frac{R}{4} \times \frac{4}{5}-R \times \frac{3}{5}=12-\frac{4}{5} R=8.06 \ldots$ | DM1 |  |
|  | Solve for $\mu: P=\mu N$, | DM1 |  |
|  | $\mu=0.630 \quad(0.63)$ | A1 |  |
|  |  |  | * could use an alternative pair of resolutions |
|  |  | [11] |  |
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